

DIVISIBILITY

÷ 2 Last digit should be even no

$$\underline{0, 2, 4, 6, 8}$$

(12)

$$1 \times 10 + 2$$

$$123 \Rightarrow 1 \times 100 + 2 \times 10 + 3$$

$$4579 \Rightarrow 4 \times 1000 + 5 \times 100 + 7 \times 10 + 9$$

$$nxyz = 1000n + 100y + 10z + 1$$

$$\frac{\cancel{4}0 + \cancel{1}2 + \cancel{1}8}{2}$$

$$\frac{\cancel{a} + \cancel{b} + \cancel{c} + \cancel{d}}{2}$$

45792 ✓

72976 ✓

75998 ✓

÷ 4 Last two digit should be divisible by 4

$$abcd = a \times 1000 + b \times 100 + c \times 10 + d$$

① 37584 ✓

⑪ 92864 ✓

⑩ 855667 ✗

798332 ✓

$$2^1 \rightarrow 1$$

$$2^2 \rightarrow 2$$

$$2^3 \rightarrow 3$$

$$2^4 \rightarrow 4$$

÷ 8 Last 3 digit should be divisible by 8

① 37324 ✓
 $\frac{324}{8} \times$

⑪ 795864 ✓
 $\frac{864}{8} \times$

⑩ 975760 ✗
 $\frac{760}{8} \times$

nxyzabc

If a is even no.

Last two digit should be divisible by 8

9 a is odd no.

add 4 in last two digits
the result should be divisible by 8

(*)

$$\cancel{675} \cancel{738}$$

$$36+4 = \frac{38}{8} X$$

$$\cancel{795} \cancel{732}$$

$$32+4 = \frac{36}{8} X$$

$$\cancel{795} \cancel{6740}$$

$$\cancel{875} \cancel{736}$$

$$36+4 = \frac{40}{8} X$$

÷ 3

sum of the digits should be divisible by 3

$$\cancel{654321} = \frac{21}{3} X$$

$$\cancel{6798552} = \textcircled{2} X$$

(*)

$$ab$$

$$10a+b$$

$$\cancel{9a} + a + b \cancel{X}$$

$$abc$$

$$100a + 10b + c$$

$$\cancel{99a} + a + \cancel{9b} + b \cancel{X}$$

$$abcd$$

$$1000a + 100b + 10c + d$$

$$1000a + 100b + 10c + d$$

$$\cancel{999a} + a + \cancel{99b} + b + \cancel{9c} + c + d$$

$$\cancel{999a} + \cancel{99b} + \cancel{9c} + a + b + c + d$$

÷ 9 sum of digits should be divisible by 9

*

$$654389 X$$

$$6+5+4+3+8+9 = \frac{35}{9} X$$

(*)

$$\checkmark 9456813$$

$$9+4+5+6+8+1+3 = 36$$

(*)

$$\checkmark 972563436$$

(*)

$$\checkmark 675827 \quad \textcircled{8}$$

$$3\cancel{5}8\cancel{1}4\cancel{6}\cancel{5}2\cancel{7}4 \quad \checkmark$$

$\div 5$ last digit should be 0 or 5

$$\div 6 \quad 6 : \cancel{2} \times 3 \quad \checkmark$$

$$\cancel{3}7\cancel{5}2\cancel{8} \times 7$$

$$\cancel{3}8\cancel{9}4\cancel{6}\cancel{7}2 \quad \begin{array}{r} 6 \\ \hline 2 \times 3 \end{array}$$

$$\div 72 \quad \begin{array}{r} 72 \\ 8 \times 9 \end{array} \quad \checkmark$$

$$\overline{\div 7} \quad \textcircled{*} \quad 75682* \quad \div 3$$

$$28 + n \quad \textcircled{7} + n = 2 \quad n = 2$$

1) $83462 * 704$ is divisible by 3, then the sum of possible digits in place of * is:

$83462 * 704$, 3 से विभाज्य हो, तो * का स्थान पर संभावित अंकों का योग है:

- (a) 17. (b) 15. (c) 16. (d) 19

$$\begin{array}{r}
 83462 * 704 \\
 \hline
 36 \quad 34 + *
 \end{array}$$

\div

$* = 2 \checkmark$
 $= 5 \checkmark$
 $= 8 \checkmark$

$2+5+8 = 15$

Calculation for possible values of *:

- $4 + * \equiv 6 \pmod{9}$ (Accepted)
- $4 + * \equiv 9 \pmod{9}$ (Rejected)
- $4 + * \equiv 12 \pmod{9}$ (Rejected)
- $4 + * \equiv 15 \pmod{9}$ (Rejected)
- $4 + * \equiv 18 \pmod{9}$ (Accepted)
- $4 + * \equiv 21 \pmod{9}$ (Rejected)
- $4 + * \equiv 24 \pmod{9}$ (Accepted)

Values of *: 2, 5, 8

2) The largest number which should replace * in the number $2365 * 4$ to make the number divisible by 4 is:

- A) 9 B) 0 C) 2 D) 8

$$2365 * 4$$

$$\begin{array}{r}
 84 \\
 88 \\
 8
 \end{array}$$

3) If the number $1005x4$ is completely divisible by 8, then the smallest integer in place of x will be:

यदि संख्या $1005x4$, 8 से पूरी विभाज्य है तो x के स्थान पर सबसे छोटा पूर्णांक होगा।

- (a) 1. (b) 0 (c) 4. (d) 2

$$\underline{1005} \times 4$$

$$\begin{array}{r} 0+4 \\ 0+4+4 \\ \hline 8 \end{array}$$

4) How many pairs of X and Y are possible in the number $\underline{763X4Y2}$, if the number is divisible by 9?

संख्या $763X4Y2$ में X तथा Y के कितने जोड़े सम्भव हैं यदि यह नंबर 9 से विभाजित होता है।

- (a) 8. (b) 9. (c) 10. (d) 11

$$\begin{array}{r} 763X4Y2 \\ \hline 4+7+X+Y \\ \hline 7+X+Y = 5 \\ \begin{array}{l} 0\ 5 \\ 5\ 0 \\ 1\ 4 \\ 4\ 1 \\ 2\ 3 \\ 3\ 2 \end{array} \end{array}$$

$$\begin{array}{r} 7+X \\ \hline 14 \\ 7+7=14 \\ \begin{array}{l} 5\ 9 \\ 9\ 5 \\ 8\ 6 \\ 6\ 8 \\ 7\ 7 \end{array} \end{array}$$

5) If 8947A56B1 is divisible by 9, where B is an odd number. Find the sum of all possible value of A?

अगर 8947A56B1, 9 से विभाज्य है, जहां B एक विषम संख्या है। A के सभी संभावित मानों का योग ज्ञात करो?

- (a) 26. (b) 27. (c) 30. (d) 36

$$8947A56B1 = \frac{22+A+B}{4+A+B}$$

$$4+A+B = 9 \quad |B| = 5$$

$$B = 1 \quad | \quad B = 3 \quad | \quad B = 5 \quad | \quad B = 7 \quad | \quad B = 9$$

$$A = 4 \quad | \quad A = 2 \quad | \quad A = 0 \quad | \quad A = 7 \quad | \quad A = 5$$

$$A = 4+2+0+9+7+5$$

B
1, 3, 5, 7, 9
 A
4, 2, 0, 7, 5

6) What is the least value of x such that $517x324$ is divisible by 12?

x का न्यूनतम मान क्या है कि $517x324$, 12 से विभाज्य है?

- (a) 3. (b) 1. (c) 0 (d) 2

$$\begin{array}{r} 12 \\ \swarrow \quad \searrow \\ 3 \times 4 \end{array}$$

$$\begin{array}{r} 517 \times 324 \\ \hline 7+0 \end{array}$$



5922

6489

380247

6891647

68761

6901895

550-550

347347

$$\begin{array}{r} \cancel{547547} \\ \cancel{7} \ 11 \ 13 \\ \hline 483 \\ -6 \\ \hline 82 \\ \hline 6891647 \\ \hline 647 \end{array}$$

$$\begin{array}{r} 891 \\ - 653 \\ \hline 238 \end{array}$$

$$\begin{array}{r} 23 \\ \times 16 \\ \hline 7 \\ \hline \end{array}$$

$$\begin{array}{r} \cancel{\div 11} \\ \times 236 \end{array} \quad \begin{array}{r} 525 \end{array}$$

2365213

$$\begin{array}{r} 10 \\ 13 \\ \hline 0.11\cancel{X} \end{array}$$

$$\begin{array}{r} 13 \\ \cancel{13} \\ \hline 0 \end{array}$$

$$X$$

$$1001 \times \$67$$

567567

005922

$$\begin{array}{r} \div 13 \\ 922 \\ 00\text{ }0 \\ \hline 917 \end{array}$$

7) 917 (B)
1/3


006 489

$$\begin{array}{r} 489 \\ \times 6 \\ \hline 483 \end{array} \quad \div 7 \quad \checkmark$$

$$\begin{array}{r} \underline{917} \\ \div 13 X \end{array}$$

$$\frac{912}{11} \div 11X$$

$$\begin{array}{r} \cancel{\text{X}} \text{ URGENT} \\ \underline{12} \\ \text{HUNIC} \\ \underline{8} \\ 36 \end{array} \div 71$$

¥ 380247

$$\begin{array}{r} 380 \\ \times 47 \\ \hline 1733 \end{array}$$

$$\begin{array}{r} \overline{)13} \quad \text{IX} \\ \cancel{13} \div \end{array}$$

$$\checkmark \quad \cancel{13} \div$$

7) What is the value of x so that the seven digit number $5656x52$ is divisible by 72?

x का मान क्या होगा कि 7-अंकीय संख्या $5656x52$, 72 से विभाज्य है?

- (a) 5. (b) 3. (c) 7. (d) 8

$5656x52$

$2 \cancel{9} + \cancel{x}2$

$11 + \cancel{x}$

$\cancel{2} + \cancel{x}2$

$$\begin{array}{r} 7^2 \\ | \\ 8 \times 9 \end{array}$$

8) What is the value of x so that the 7-digit number $91876x2$ is divisible by 72?

x का मान क्या होगा कि 7 अंकीय संख्या $91876x2$, 72 से विभाज्य है?

- (a) 2. (b) 7. (c) 6. (d) 3

$918\cancel{7}6x7$

$$6 + \cancel{x} = 9$$

$$\cancel{x} = 3$$

$$\begin{array}{r} 7^2 \\ | \\ 8 \times 9 \end{array}$$

9) If a 9-digit number $389x6378y$ is divisible by 72, then the value of $\sqrt{6x + 7y}$ will be:

यदि एक 9- अंकीय संख्या $389x6378y$ m, 72 से विभाज्य है, तो $\sqrt{6x + 7y}$ का मान होगा:-

- A) 8 B) 6. C) 9. D) 10

$$389 \times 6378 \underline{\underline{y}}$$

$$\begin{aligned} &389 \times 6378^y \\ &3+n \Rightarrow \\ &n=6 \end{aligned}$$

$$\begin{aligned} &\begin{array}{c} 72 \\ \sqrt{6n+7y} \\ 8 \times 9 \\ 8 \times 4 \\ n=6 \\ \hline \end{array} \\ &\begin{array}{r} 72 \\ 80 \\ 88 \\ \hline \end{array} \\ &\begin{array}{l} \sqrt{6n+7y} \\ = \sqrt{6 \times 6 + 7 \times 8} \\ \sqrt{36+56} = \sqrt{92} \approx 8 \end{array} \end{aligned}$$

10) If 11-digit number $5678x43267y$ is divisible by 72, then the value of $\sqrt{5x + 8y}$ is

यदि 11- अंकीय संख्या $5678x43267y$, 72 से विभाज्य है, तो $\sqrt{5x+8y}$ का मान होगा:

- (a) 4. (b) 6. (c) 7. (d) 8

$$5678 \times 43267 \underline{\underline{y}}$$

$$\begin{aligned} &5678 \times 43267 \underline{\underline{y}} \\ &\underline{23+2} = 5+2 \\ &n=4 \end{aligned}$$

$$\begin{aligned} &\begin{array}{c} 72 \\ \sqrt{5n+8y} \\ 8 \times 9 \\ 8 \times 4 \\ n=4 \\ \hline \end{array} \\ &\begin{array}{r} 72 \\ 56 \\ 36 \\ \hline \end{array} \\ &\begin{array}{l} \sqrt{5n+8y} \\ = \sqrt{5 \times 4 + 8 \times 2} \\ \sqrt{20+16} = \sqrt{36} \\ = 6 \end{array} \end{aligned}$$

11). If 10-digit number $5432y1749x$ is divisible by 72 then what is the value of $(5x - 4y)$

यदि 10- अंकीय संख्या $5432y1749x$, 72 से विभाज्य है, तो $(5x - 4y)$ का मान होगा:

- (a) 9. (b) 10. (c) 14. (d) 15

$$\begin{array}{r}
 \text{543241749} \\
 - \text{543271749} \\
 \hline
 \text{5+8=9} \\
 \text{y=4}
 \end{array}
 \quad
 \left| \begin{array}{l}
 x = 6 \\
 \hline
 \text{72} \\
 \text{5x6=4x4} \\
 \text{30-16} \\
 \hline
 \text{=14}
 \end{array} \right.$$

12) If the 10-digit number $897359y7x2$ is divisible by 72, then what is the value of $(3x + y)$ for the possible greatest value of y ? ↗

यदि 10 अकों का संख्या $897359y7x2$, 72 से विभाज्य है, तो y को संभावित सबसे बड़े मान के लिए $(3.xry)$ का मान क्या है?

- (a) 23. (b) 28. (c) 27. (d) 25

$$\begin{aligned}
 8 &+ 7 + 3 + 5 = 23 \\
 s + n + g &= 9 \\
 n + g &= 4 \\
 1 + g &= 4 \\
 g &= 3
 \end{aligned}$$

$$\begin{array}{r}
 x = 1 \\
 + 5 \\
 \hline
 = 9
 \end{array}$$

$x + y = 18$

$$\begin{array}{r}
 x + y = 13 \\
 - \quad \quad \quad \\
 \hline
 y = 8
 \end{array}$$

$$\begin{array}{r}
 x + y = 13 \\
 - 8 \\
 \hline
 y = 5
 \end{array}$$

$$\begin{array}{r}
 72 \\
 \times 8 \\
 \hline
 56
 \end{array}$$

$$\begin{array}{r} 3x + 8 \\ 3 \times 5 + 8 \\ 15 + 8 \\ \hline 23 \end{array}$$

13) For what value of x is the seven-digit number $46393x8$ divisible by 11?

x के किस मान के लिए सात अंकों की संख्या $46393x8$, 11 से विभाज्य है

- (a) 5. (b) 3 (c) 2 (d) 7

$46393x8$

$$\begin{array}{r} 18 \\ 15+8 \end{array}$$

14) What should replace in the number 94^*2357 , so that number is divisible by 11?

संख्या 94^*2357 में को किस अंक से प्रतिस्थापित करना चाहिए, ताकि वह संख्या 11 से विभाज्य हो?

- (a) 1. (b) 7. (c) 8. (d) 3

94^*2357

$$\begin{array}{r} 19+* \\ 11 \\ \hline 22 \\ -11 \\ \hline 11 \end{array}$$

$* = 3$

15) If 738A6A is divisible by 11, then the value of A is.

- A) 6. B) 3. C) 9 D) 4

$$\begin{array}{r}
 738\text{A}6\text{A} \\
 \div 11 \\
 \underline{21} \\
 3+2A \\
 \underline{21-3-2A=0} \\
 18 = 2A \\
 \textcircled{6}
 \end{array}$$

16) If digit number $\underline{x}35624$ and $\underline{1257y4}$ are divisible by 11 and 72, respectively, what is the value of $(5x - 2y)$?

यदि छह अंकों वाली संख्याओं $x35624$ और $1257y4$ क्रमशः 11 और 72 से विभान्यय हैं तो $(5x - 2y)$ का मान क्या होगा?

- (a) 14 (b) 12. (c) 10. (d) 13

$$\begin{array}{r}
 \underline{\underline{x35624}} \\
 \underline{\underline{1257y4}}
 \end{array}
 \left| \begin{array}{r}
 \begin{array}{r}
 7+x \\
 \hline
 13 \\
 n=6
 \end{array}
 & \begin{array}{r}
 5n-2y \\
 1+7=9 \\
 8=8
 \end{array}
 \end{array} \right.$$

$$\begin{array}{r}
 5n-2y \\
 5 \times 6 - 2 \times 8 \\
 30 - 16 = 14
 \end{array}$$

$$\begin{array}{r}
 5n-2y \\
 1257y4 \\
 1+7=9 \\
 8=8
 \end{array}
 \left| \begin{array}{r}
 72 \\
 8 \times 9
 \end{array} \right.$$

17) If the nine-digit number $708x6y8z9$ is divisible by 99, what is the value of $x+y+z$?

यदि 708x6y8z9 वाली नौ अंको वाली संख्या 99 से विभाज्य है, तो $x+y+z$ का मान क्या है?

- (a) 27. (b) 5. (c) 16. (d) 9

$$\begin{array}{r} 708x6y8z9 \\ \underline{- (x+y+z)} = 0, 11, 22 \end{array}$$

$$\begin{array}{r} 38 \\ 27 \\ \hline 11 \end{array}$$

18) If the 6-digit number is $15x1y2$ is divisible by 44, then $(x+y)$ is equal to:

यदि 6 अंकीय संख्या $15x1y2$, 44 से विभाज्य है, तो $(x + y)$ बराबर है:-

- (a) 8. (b) 7. (c) 6 (d) 9

$$x = 1$$

$$\begin{array}{r} 15x112 \\ 2+n \\ \hline 8 \\ n=6 \end{array}$$

$$\begin{array}{r} \div 44 \\ 4 \times 11 \end{array}$$

$$\begin{array}{l} x=1 \\ y=8 \end{array}$$

$$\begin{array}{r} 15x182 \\ 9+n \\ -8 \\ \hline 9+n-8=11 \\ 9+n=19 \\ n=10 \end{array}$$

19) What is the value of x so that the 7-digit number 6913x08 is divisible by 88?

7 अंकीय संख्या 6913x08, 88 से विभाज्य है तब x का मान है?

- (a) 4. (b) 2. (c) 8. (d) 6

$$\begin{array}{r}
 \text{6} \underset{\text{15+x}}{\text{9}} \text{1} \underset{\text{12}}{\text{3}} \times \text{0} \text{8} \quad \div 88 \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 15 + x \\
 \hline
 12 \\
 15 - 12 = 3 \\
 3 + x \equiv 11 \\
 x = 8
 \end{array}$$

20) If the 8-digit number 2074x4y2 is divisible by 88 then the value of (4x + 3y) is

यदि 8 अंकीय संख्या 2074.x4y2, 88 से विभाज्य है, तो (4x + 3y) बराबर है:-

- (a) 49. (b) 36. (c) 42. (d) 45

$$\begin{array}{r}
 2074 \times 4y2 \\
 \hline
 9 + n + y - 10 = 0, 11 \\
 9 + n + y - 10 = 0 \\
 n + y = 1 \\
 9 + n + y - 10 = 11 \\
 n + y = 12
 \end{array}$$

$$\begin{array}{ll}
 \text{when } y = 3 & y = 7 \\
 n = 9 & n = 5 \\
 4n + 3y & \\
 4 \times 9 + 3 \times 3 & \\
 36 + 9 = \underline{45} &
 \end{array}$$

$$\begin{array}{r}
 88 \\
 \hline
 8 \times 11 \\
 4y2 \\
 \hline
 8 \\
 y = 3, 87
 \end{array}$$

$$\begin{array}{r}
 4n + 3y \\
 4 \times 9 + 3 \times 7 \\
 20 + 21 = \underline{41}
 \end{array}$$

21) What is the least value of x such that $517x324$ is divisible by 12?

x का न्यूनतम मान क्या है कि $517x324$, 12 से विभाज्य है?

- (a) 3. (b) 1. (c) 0. (d) 2

$$8/17 \times 324$$

$7+2$

$\begin{array}{r} 12 \\ \times 3 \times 4 \\ \hline \end{array}$

22) If 11-digit number $543247x968y$ is divisible by 90, then the value of $(4x + 5y)$

यदि 11 अंकों की संख्या $543247x968y$, 90 से विभाज्य है, तो $(4x + 5y)$ का मान है।

- (a) 24. (b) 21. (c) 25. (d) 16

543247×9683 $\underline{\quad 90 \quad}$

543247×9684 $y =$

543247×9680 $3+n = \textcircled{n=6}$

$4n+5y$

$4 \times 6 + 5 \times 0$

$\textcircled{24}$